

## Retake Mastermath course 'Scheduling' 2019

8-7-2019

The exam consists of 5 questions worth 10 points each. Your grade is given by  $1 + \frac{9p}{50}$ , where  $p$  is the total number of points obtained.

Note: You are only allowed to use the handout written by the lecturers. **Good luck!**

### Question 1 (10 points):

Consider the following instance of problem  $J2||C_{max}$ :

$n = 6$ ,  $p = \begin{pmatrix} 2 & 9 & 5 & 1 & 3 & - \\ 4 & 4 & 2 & 6 & - & 3 \end{pmatrix}$ , jobs 1 and 2 have to be processed first on  $M_1$ , jobs 3 and 4 have to be processed first on  $M_2$ .

Apply the presented optimal algorithm for problem  $J2||C_{max}$  to this instance. Explain the different steps, give the results of these steps and present the optimal solution.

### Question 2 (10 points):

Consider problem  $1|d_j = d|\sum T_j$  (minimize total tardiness if all jobs have equal due date  $d$ ).

Give a scheduling rule that leads to an optimal solution and proof that an optimal schedule can be found by this rule.

### Question 3 (10 points):

Proof that problem  $P2||\sum w_j C_j$  is NP-hard.

### Question 4 (10 points):

Consider problem  $P||C_{max}$ .

Give the maximal number of jobs (dependent on the number  $m$  of machines) for which LPT leads always to an optimal solution and prove that this is true.

### Question 5 (10 points, indication 300 words):

Give a general description of different variants of the charging problem for electric vehicles. Describe the problems including objectives and constraints. Furthermore, give a sketch of the solution approach for the basic variant of the problem.

END OF THE EXAM