UNIVERSITY OF TWENTE

Department of Electrical Engineering, Mathematics and Computer Science

Exam Signals and Transforms on Tuesday March 28, 2017, 8.45 - 10.15 hours.

The solutions of the exercises should be clearly formulated. Moreover, in all cases you should motivate your answer!

You are not allowed to use a calculator. Besides pen and paper, the only thing you are allowed to use is one handwritten, singe-sided, A4-sized page of personal notes.

1. Consider a filter whose step response is given by:

$$g(t) = e^{-(2t+1)^2}$$

a) Show that the Fourier transform of the step response is equal to:

$$\hat{g}(\omega) = \frac{\sqrt{\pi}}{2e} e^{\frac{1}{16}(i\omega+4)^2}$$

- b) Determine the frequency response
- c) Consider the input:

$$u(t) = \mathbb{1}(t+1) + 2\delta(t)$$

Compute the corresponding output y(t).

d) Consider the input:

 $u(t) = \cos(4t)$

Compute the corresponding output y(t) and show it is real-valued.

- 2. Determine the convolution of $f(t) = e^{-t} \mathbb{1}(t)$ and $g(t) = \mathbb{1}(-t)$ via Fourier or Laplace transformation.
- 3. Given is the differential equation:

$$y^{(2)}(t) - 7y^{(1)}(t) + 12y(t) = u^{(1)}(t) - 2u(t).$$
⁽¹⁾

- a) Determine the impulse response of (1).
- b) Determine the step response of (1).
- c) As input we choose $u(t) = e^t \mathbb{1}(t)$. Determine the solution for t > 0 of (1) with $y(0^-) = 1$, $y'(0^-) = -1$.

For the exercises the following number of points can be obtained:

Exercise 1. 10 points Exercise 2. 7 points Exercise 3. 10 points The grade is determined by adding 3 points to the total number of points obtained and dividing by 3.